



Performance assessment of daily GR conceptual rainfall-runoff models in the Upper Benue River (Cameroon) using airGR packages

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Abstract. Many hydrological applications employ conceptual-lumped rainfall-runoff models to support water resource management techniques. Because of their ability to exploit minimal data and provide enough credible information, they provide an edge in data-scarce domains. The purpose of this research is to evaluate the feasibility of using multiple rainfall-runoff hydrologic models Génie Rural à 4, 5, 6 paramètres Journalier (GR4J, GR5J, and GR6J) in the Upper Benue River (UBR) in Northern Cameroon. The models were calibrated using Michel's calibration algorithm implemented in airGR packages, while considering different objective functions (NSE, KGE, composite criterion). The objective here was to find the optimum objective function that takes into account the various components of the hydrographs in this watershed and to assess the impact of the chosen objective function on parameter optimization. The results reveal that the model performance as well as the optimized parameters of the different GR models vary according to the selected objective function. According to the study, adopting the composite criterion as an objective function during model calibration improves model accuracy. The model's performance reveals that two of the three models (GR5J and GR6J) reproduced the discharge well in the considered catchment, with NSE and KGE greater than 0.62 during the model validation. This highlights how these two GR models can be applied to various water management concerns in the UBR.

Keywords. UPH 19; Open Science; Modelling; GR hydrological models, airGR packages

1 Introduction

Nowadays, hydrological models are essential and powerful tools for the efficient management of water resources. They are used to simulate the different hydrological processes occurring at the watershed scale, to prevent extreme events such as floods and droughts, and are now widely used to study the impacts of climate change and land cover on water resources at the global, regional and local scales (Tshimanga and Hughes, 2012; Nonki et al., 2019, 2021b; Lemaitre-Basset et al., 2021). A large number of hydrological models that vary from physical-based to conceptual models are currently available. But the choice between the distributed, semi-distributed and lumped-conceptual is very important for catchment hydrology. Given the greediness of semi-distributed and distributed models in terms of input data, conceptual-lumped rainfall-runoff models are the most commonly used especially in the context of data-scarce regions (Tegegne et al., 2017). They have the advantage that they can use limited data and generate sufficiently reliable information (Nonki et al., 2021c). They are also usually simple and relatively easy to implement.

They are GR (Génie Rural) models in terms of the number of extant and extensively used conceptual-lumped models (Perrin et al., 2009). The GR models were developed in the early 1980s by Claude Michel at Irstea, a French national applied research institute. Nowadays, there are numerous GR models that differ in terms of both time-step (annual, monthly, daily, and hourly) and the number of free model parameters. Because these models are rather parsimonious, end users can easily code them in their modeling environment. However, providing the models in a default implementation environment can make them easier to use and ensure their correct application. Coron et al. (2017) built the airGR packages in this context, which make the GR models available in R. They provided a GR simulation tool that is free, open source and easy to disseminate. Based on their accuracy to simulate discharge around the world and especially in the African catchments, this study aims to assess the feasibility of applying daily GR models in the Upper Benue River for future water resources management.

2 Materials and methods

2.1 Study area and data

The study is conducted in the Upper Benue River (UBR) located in northern Cameroon between latitudes 7 and 11° N, and Longitudes 12 and 16° E (Fig. 1). It is Cameroon's second largest river with a watershed of 64 000 km² at Garoua outlet and serves as the main tributary to the Niger River basin. This basin rises in the Adamaoua Plateau and constitutes the most socioeconomic economic impediment of the Northern region because of its potential for sustaining various water-related activities such as irrigated agriculture, hydroelectricity production and navigation. A tropical climate prevails in the basin with two main seasons: the rainy season lasts from May to October and the dry season from November to April. It's a unimodal rainfall region (maximum in August) with annual rainfall ranges between 900 and 1500 mm (Dassou et al., 2016). The prevailing vegetation type in the region is savanna, and elevation is characterized by three main hills: the Adamawa Plateau, and Mounts Alantika and Mandara.

Daily meteorological and hydrological data were used in this study to calibrate and validate the hydrological models. The meteorological data consisted of precipitation obtained from 25 stations and potential evapotranspiration (PET) computed by Penman's formula (Penman, 1948) from solar radiation, relative humidity, wind speed at 2 m, as well as minimum, maximum and average air temperatures from 4 stations located in the basin. These data were provided by the Direction of the National Meteorology of Cameroon (DNM). The daily measured discharge at the Garoua gauging stream station were obtained from the Système d'Information Environnementales sur les Ressources en Eaux en Afrique pour leur Modélisation (SIEREM) database of HydroSciences Montpellier (Boyer et al., 2006; http://www.hydrosciences.org/ index.php/2020/08/26/bases-de-donnees/, last access: 1 May 2023).

2.2 Hydrological models description

Three daily time-step GR (Génie Rural) lumped-conceptual rainfall-runoff models were used: the GR model with four daily parameters (GR4J; Perrin et al., 2003), the GR model with five daily parameters (GR5J; Le Moine, 2008), and the GR model with six daily parameters (GR6J; Pushpalatha et al., 2011). To simulate discharge, these models use daily precipitation and PET as inputs. The GR5J is a modified version of the GR4J that includes an additional parameter (X_5) . It is a threshold for inter-catchment exchange (-) which can take positive or negative values. While GR6J is an upgraded version of GR5J which incorporates an additional routing store (X_6 : exponential store controlling parameter, mm) that allows more flexibility for low-flow modeling (Coron et al., 2017). Figure 2 depicts a schematic view of the various hydrological processes accounted for in the various models, where X_1 is the maximum capacity of the production store (mm), X_2 is the groundwater exchange coefficient (mm), X_3 is the maximum capacity of the routing store (mm) and X_4 is the base time of unit hydrograph (days).



Figure 1. Study catchment: basin drainage area and rainfall and hydrological stations.



Figure 2. Schematic view of the different hydrological processes accounted for in the GR4J, GR5J and GR6J Conceptual-Lumped hydrological models.



Figure 3. Observed precipitation at the UBR (upper panel), observed vs. simulated daily discharge at the UBR (Garoua hydrometric station) using the GR6J model (middle and lower panels) during the calibration (1961–1970).

2.3 Model calibration, validation and performance assessment

The split - Sample test (Klemeš, 1986) was used for model calibration and validation. Our data time-series were divided into two sub-periods: calibration from 1 January 1961 to 31 December 1970 and validation from 1 January 1971 to 31 December 1980. Calibration/validation was repeated twice, by swapping the two periods (the second half for calibration and first half for validation). By doing this, we can get rid of the dependency of model performance to the simulated period. The model was calibrated using Michel (1991)'s optimization algorithm. These model parameters were calibrated against three different objective function: the Nash and Sutcliffe Efficiency (NSE; Nash and Sutcliffe, 1970), the Kling-Gupta efficiency (KGE; Gupta et al., 2009) and the composite criterion (OF; Lemaitre-Basset et al., 2021) that allowed a fair compromise of both low and high flows. It's the average KGE value, calculated with discharge and inverse of discharge series. The formulation of the two first criteria can be found in Nonki et al. (2021a, c) and the last criterion is given in Eq. (1):

$$OF = \frac{KGE(Q) + KGE(1/Q)}{2}$$
(1)

The model's performance was assessed by using both graphical (hydrographs of observed and simulated discharge and flow duration curves) and statistical criteria such as NSE with its different transformations (log and sqrt), KGE, root mean square error (RMSE) and Pearson correlation coefficient (r).

3 Results and analysis

3.1 Impact of selected objective function on optimized parameters and performance

Table 1 gives the optimized model parameters and the performance criteria obtained during the model calibration using different objective functions. The results reveal that the optimum model parameters for the three models differ depending on the criterion used. This result was rather predictable given that we trained the model for different purposes. We also notice that the use of a composite criterion as an objective function during model calibration is highly recommended due to its ability to account both low and high flows components (represented by NSE(log Q) and NSE(\sqrt{Q}) respectively) compared to NSE and KGE in which the models fail to simulate low flows. This result corroborates with those of Garcia et al. (2017) which recommended using OF as an objective function to simulate low-flow indices with continuous conceptual rainfall-runoff models. Despite the fact that increasing model parameters number increase the model uncertainty, we found that increasing the number of model parameters improves model accuracy. This means that the addition of one process to the model improve its performance.

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Table 1. Optimized parameters and performance criteria using different objective functions during the calibration period (1961–1970).

Models Objective function		GR4J			GR5J			GR6J		
		NSE	KGE	OF	NSE	KGE	OF	NSE	KGE	OF
Model	<i>X</i> ₁	120.76	59.4	162	257.96	175.92	0.03	5.35	72.9	0.01
parameters	X_2	1.15	-4.21	-0.93	-0.12	-0.57	-2.66	-1.14	-0.52	-0.95
	X_3	16.20	268.57	22.75	34.38	130.32	239.20	251.52	101.67	170.59
	X_4	6.80	6.68	2.49	6.67	5.24	6.22	6.59	7.24	6.41
	X_5				1.0	0.367	0.09	0.20	0.22	0.01
	X_6							16.38	14.21	7.30
Performance	NSE(Q)	0.84	0.86	0.36	0.84	0.83	0.82	0.87	0.85	0.80
criteria	$NSE(\sqrt{Q})$	0.80	0.87	0.66	0.79	0.82	0.90	0.85	0.85	0.90
	$NSE(\log Q)$	0.21	0.47	0.60	0.17	0.28	0.87	0.36	0.40	0.87
	KGE(Q)	0.87	0.93	0.63	0.89	0.91	0.90	0.86	0.92	0.88
	KGE(1/Q)	-0.39	-0.31	0.17	-0.44	-0.40	0.45	-0.29	-0.50	0.43
	OF	0.24	0.31	0.40	0.23	0.26	0.67	0.29	0.29	0.65



Figure 4. Same as Fig. 3 but during the validation period (1971–1980).

3.2 Models' evaluation results

To evaluate the model performance, we used the optimized model parameters obtained using composite criterion as objective function. Figures 3 and 4 show the comparison between the observed and simulated hydrograph as well as flow duration curves during the calibration and validation using the GR6J model. It's clear that the model captures the timing and magnitude of the discharge well in the UBR. In addition, the model well captured the annual cycle of discharge. However, we also notice that the model fails to simulate the low flows compared to high flows. The same results are achieved with GR5J although they differ slightly with GR4J (Figures not shown).

These findings are reinforced by multi-statistical criteria analysis shown in Table 2. Calibration and validation of the models within the same sub period reveal that the model performed better during model calibration. This result is not surprising as the model is calibrated to better depict the watershed's hydrologic conditions during the calibration period, which are never exactly the same throughout model validation (Merz et al., 2009). In addition, the models outperform during the first half of the calibration period and during the

Model		Period	NSE(Q)	$NSE(\sqrt{Q})$	$NSE(\log Q)$	KGE(Q)	KGE(1/Q)	OF	RMSE	R^2
GR4J	Calibration	1961-1970	0.36	0.66	0.60	0.63	0.18	0.40	0.76	0.73
		1971–1980	0.27	0.64	0.40	0.59	-0.03	0.28	0.61	0.73
		Mean	0.32	0.65	0.50	0.61	0.075	0.34	0.685	0.73
	Validation	1961–1970	0.40	0.61	0.24	0.54	-0.89	-0.18	0.74	0.71
		1971–1980	0.12	0.67	0.64	0.55	-0.23	0.16	0.67	0.71
		Mean	0.26	0.64	0.44	0.545	-0.56	-0.01	0.705	0.71
GR5J	Calibration	1961–1970	0.82	0.90	0.87	0.90	0.44	0.67	0.40	0.92
		1971–1980	0.75	0.75	0.36	0.81	0.00	0.40	0.36	0.89
		Mean	0.785	0.825	0.615	0.855	0.22	0.535	0.38	0.905
	Validation	1961–1970	0.79	0.76	0.20	0.72	-0.98	-0.13	0.44	0.90
		1971–1980	0.65	0.86	0.84	0.62	-0.09	0.26	0.43	0.90
		Mean	0.72	0.81	0.52	0.67	-0.535	0.065	0.435	0.90
GR6J	Calibration	1961–1970	0.80	0.90	0.87	0.88	0.43	0.65	0.42	0.91
		1971–1980	0.79	0.88	0.63	0.87	0.05	0.46	0.33	0.91
		Mean	0.795	0.89	0.75	0.875	0.24	0.555	0.375	0.91
	Validation	1961–1970	0.81	0.87	0.67	0.75	-0.89	-0.07	0.42	0.91
		1971–1980	0.66	0.87	0.80	0.65	-0.12	0.27	0.42	0.90
		Mean	0.735	0.87	0.735	0.70	-0.505	0.1	0.42	0.905

Table 2. Statistical summary of the model performance of the three daily GR models during the calibration and validation periods at the Benue River (Garoua hydrometric station). The models were calibrated using OF as objective function.

second half of the validation period. The GR5J and GR6J models clearly outperformed the GR4J model in the UBR. This can be explained by the fact that Northern Cameroon is a semi-arid region in Cameroon where many rivers dry up a few months after the rainy season, then the groundwater significantly contributes to the stream flow during the dry season. Therefore, the better the groundwater exchange is taken into account in the hydrological model, the better the accuracy is. An objective examination demonstrates that the GR6J model outperforms the other two models. This finding is consistent with earlier research (Flores et al., 2021; Tyralis et al., 2023).

4 Conclusions

The aim of this study was to assess the viability of applying daily GR Conceptual-Lumped models in the Upper Benue River for future water management challenges. We used the airGR packages in R, which give GR models. The Michel's algorithm implemented in these packages was used for model optimization using three different objective criteria, and the model's performance was evaluated using different statistical criteria. The results showed that the optimized parameters vary according to the selected objective function and suggested the use of composite criteria as an objective function during the model calibration. In addition, the GR5J and GR6J models outperformed the GR4J model. This demonstrates that adding one reservoir to the model for groundwater simulation outperforms the model. **Code and data availability.** This study was conducted using airGR packages available online (https://CRAN.R-project.org/ package=airGR, Coron et al., 2023). Meteorological and hydrological data are the properties of the Direction of the National Meteorology of Cameroon (DNM) and the SIEREM/HSM database respectively. Interested users can contact the corresponding author to have access to the data.

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