

An aerodynamic approach in soil hydraulic conductivity estimation for investigating soil erosion degree

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Abstract We propose a new method for determining the degree of erosion for zonal soils of the East European Plain. This new approach uses soil porosity and filtration to determine a coefficient of aerodynamic similarity. We evaluated the degree of soil erosion on ranges of the major zonal soils of the eastern part of European Russia by applying this new method. Based on these data, we developed a diagnostic scale to determine the extent of soil erosion in this area.

Key words surface erosion; soils; filtration coefficient; porosity; diagnostic scales.

INTRODUCTION

Surface soil erosion is a ubiquitous feature of our landscape. Water flow from rain, snow and spring thaw transport and deposit soil, often unpredictably. Most surface soil erosion occurs in agricultural areas. As no universal criteria for the determination of the severity of erosion exists, we generated a method by which soil surface erosion may be quantified. A number of methods for soil porosity measurement are known: Richards (1931), Kraus *et al.* (1953), Sirotkin & Ginzburg (1971), Dullien (1991), and Stewart *et al.* (2013). These methods may be performed in a laboratory environment, or in the field, by determining the capillary porosity or aeration (Onishchenko, 1986). In contrast to these methods, we propose a new method of measuring total porosity that does not require the solid phase density measurement. Therefore, our new method may be used for undisturbed soils without excessive water content.

METHOD DEVELOPMENT

This method is based on the isothermal expansion of air trapped in soil pores when the soil sample is set within a vacuum. A sample of undisturbed soil with a set volume, V_{soil} , is placed in the vessel 1 of V_1 volume. Vessel 1 is connected by a vacuum gauge to vessel 2 of a known volume, V_2 . Vessel 2 is then connected to an atmosphere or a vacuum pump. Both vessels are then sealed. Vessel 1 is split-off by taps set in vessel 2 at p_2 vacuum. Vessel 1 and the sample have p_1 pressure, equal to 1 atmosphere. Both vessels are then connected and the expansion of air from the sample contained within vessel 1 flows into vessel 2. A common pressure p will then be established for the system.

Using the Clapeyron-Mendeleev law, the following formulae are obtained:

$$p_1 V_1 = \frac{m_1}{\mu} RT_1 \quad \text{– for the first vessel} \quad (1)$$

$$p_2 V_2 = \frac{m_2}{\mu} RT_2 \quad \text{– for the 2nd vessel} \quad (2)$$

$$p(V_1 + V_2) = \frac{m_1 + m_2}{\mu} RT \quad \text{– for the whole system} \quad (3)$$

where m_1 is the mass of gas in the first vessel; m_2 is the mass of gas in the second vessel; R is a universal gas constant; T_1 , T_2 , T are the temperatures in the first and second vessels and in the entire system; μ is the molar mass of air.

Assuming the process is an isothermal one, i.e.:

$$T_1 = T_2 = T \quad (4)$$

equations (1), (2), (3) express the pressure p , which is read on the vacuum meter after the vessel connection:

$$p = (p_1V_1 + p_2V_2) / (V_1 + V_2) \quad (5)$$

V_1 volume consists of the soil-ground volume, V_{por} , and volume V_1 , which is determined experimentally on the same apparatus by replacing the non-porous soil-ground sample with a non-porous body of the same volume. After transformation, the following formula may be obtained:

$$V_{por} = \frac{V_2(p_2 - p) + V_1(p_2 - p)}{p - p_1} \quad (6)$$

whereby V_{por} is the pore volume in the sample occupied by air.

At a parallel measurement of humidity, the volume of moisture within the soil pores, V_{water} , may be calculated. Thus, the total porosity of the sample makes:

$$P = (V_{pores} + V_{water}) / V_{soil}. \quad (7)$$

Substituting the obtained value of porosity from equation (7) and the experimentally determined value of the bulk density, it is possible to estimate the density of the solid phase for an undisturbed sample:

$$p_s = p_v / (1 - P) \quad (8)$$

In our study, soil samples of about 500 cm³ were collected. Air pressure transmitted through the sample was measured with a vacuum gauge from the exhaust meter mark of 0.05 atm, which allowed measurement of the porosity of the same sample with five repeats giving an average relative error of less than 1%, and for different specimens of the same depth at a distance of 0.5 m apart with a maximum error of about 2%.

The sample humidity was determined by a thermostatic-gravimetric method. The proposed method of measuring the porosity and density of the soil solid phase is used in the field conditions with a portable vacuum pump.

The infiltration coefficient was determined using computational methods based on the measurements of other variables, the determination of which, according to the authors, is more reliable, convenient and secure with methodological and technical aspects.

We used aerodynamic method of hydraulic conductivity determination (coefficient of hydraulic conductivity) for a generalized description of the relationship between permeability factor and humidity for large groups of dispersed systems.

Continuous media stream as it moves through a porous system is determined by Darcy's law:

$$Q = K \frac{\Delta P}{\Delta x} S_s \quad (9)$$

Using an idealized model (Fig. 1) of soil partials, a soil sample may be replaced in calculation by a direct cylinder tube of an effective radius, the length of which is equal to the sample length, and the energy loss when the continuous medium is flown through it is equal to the energy losses at the flow of the same medium through the same sample. For this tube current the flow is determined by the Poiseuille equation:

$$Q = \frac{\pi}{8\eta} \frac{\Delta P}{\Delta x} R_{ef}^4 \quad (10)$$

Equation (10) corresponds to the case when the soil-ground portion of the soil-ground space is occupied by moisture, i.e. the numerical values of Q , ΔP , R_{ef} are obtained from the air flow experiment described above. For the case of moisture lack in pores, the same equation will be as follows:

$$Q_0 = \frac{\pi}{8\eta} \frac{\Delta P}{\Delta x} R_{0ef}^4 \quad (11)$$

where the values of Q_0 , R_{0ef} correspond to the dry sample. When the sample humidity is changed the air consumption rate flowing through it decreases with moisture volume increase. This flow rate change is determined by the expression formulated for a special case with the measured value R_{ef} .

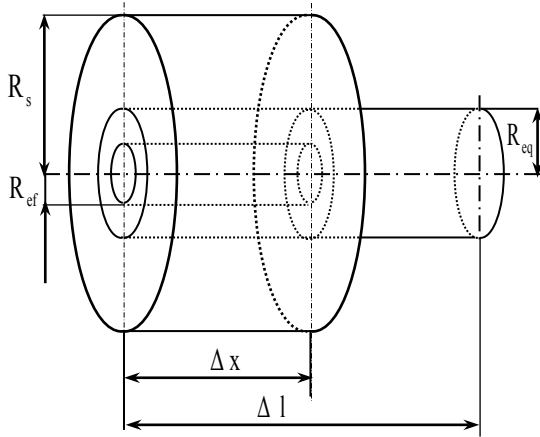


Fig. 1 An idealized model of soil. R_s is the radius of the sample, R_{ef} is the effective radius, the radius of the sample flow tube, where gas flow Q is equal to the gas flow through the sample at the same pressure gradient, R_{eq} - equivalent radius, Δx is sample length, Δl is the length of the tube with equivalent radius, the energy losses are equal to the flow in the tube of the effective radius and thus losses in the air flow through the sample.

$$\Delta Q = Q_0 - Q = \frac{\pi}{8\eta} \frac{\Delta P}{\Delta x} (R_{0ef}^4 - R_{ef}^4) \quad (12)$$

The same change of consumption ΔQ can be formally represented in the form of Darcy's law:

$$\Delta Q = K' \frac{\Delta P}{\Delta x} S_s \quad (13)$$

where ΔQ is an air consumption rate through the cylindrical layer of thickness $\Delta h = R_{0ef} - R_{ef}$; K' is the air permeability coefficient through this layer.

Equating (12) and (13) we obtain the following formula:

$$\frac{\pi}{8\eta} (R_{0ef}^4 - R_{ef}^4) = K' S_s \quad (14)$$

When the air permeability coefficient K' is expressed from (14), we obtain:

$$K' = \frac{\pi (R_{0ef}^4 - R_{ef}^4)}{8\eta S_s} \quad (15)$$

The air consumption through the flow tube of a measured effective radius corresponding to the wet sample R_{ef} , and the air flow through the flow tube of the same length with an effective radius R_{0ef} , corresponding to dry sample are different and described by the following equations:

$$\frac{\Delta V}{\Delta t} = \frac{\pi}{8\eta} \frac{\rho g \Delta h}{\Delta x} R_{ef}^4 \quad (16)$$

$$\frac{\Delta V}{\Delta t_0} = \frac{\pi}{8\eta} \frac{\rho g \Delta h_0}{\Delta x} R_{0ef}^4 \quad (17)$$

Expressing the corresponding effective radii from equations (16) and (17) the following equations are obtained:

$$R_{ef}^4 = \frac{\Delta V 8\eta \Delta x}{\Delta t \Delta h \rho g \pi} \quad (18)$$

$$R_{0ef}^4 = \frac{\Delta V 8\eta \Delta x}{\Delta t_0 \Delta h_0 \rho g \pi} \quad (19)$$

or, given that the air volume of ΔV is a constant, we obtain:

$$\frac{R_{ef}^4}{R_{0ef}^4} = \frac{\Delta t_0 \Delta h_0}{\Delta t \Delta h} \quad (20)$$

which includes two uncertain values, R_{0ef} and $\Delta t_0 \Delta h_0$, which are used to define the concept of equivalent radii.

Equivalent radius in this model can be defined as the radius of a single cylindrical pore with the length of Δx , the volume of which is equal to the total pore volume of the sample.

Writing the Poiseuille equations for flow tubes of equivalent radii R_{0eq} and R_{eq} , aerodynamically, similar to the relevant flow tubes with R_{0ef} and R_{ef} radii of the same length Δl , we obtain the following formulations:

$$Q = \frac{\pi}{8\eta} \frac{\Delta P}{\Delta l} R_{eq}^4 \quad (21)$$

$$Q_0 = \frac{\pi}{8\eta} \frac{\Delta P}{\Delta l} R_{0eq}^4 \quad (22)$$

Using arguments similar to the above, we obtain:

$$\frac{R_{eq}^4}{R_{0eq}^4} = \frac{\Delta t_0 \Delta h_0}{\Delta t \Delta h} \quad (23)$$

where:

$$\Delta t_0 \Delta h_0 = \Delta t \Delta h \frac{R_{ef}^4}{R_{0ef}^4} \quad (24)$$

Equivalent radii are found from the following equations:

$$P = \frac{R_{eq}^2}{R_s^2} \quad (25)$$

$$P_0 = \frac{R_{0eq}^2}{R_s^2} \quad (26)$$

where R_s is the sample radius, P and P_0 are the porosity in wet and dry conditions, respectively. P is determined experimentally, while P_0 is calculated by:

$$P_0 = W_v + P, \quad (27)$$

where W_v is volumetric moisture in unit fractions, i.e. the value measured experimentally.

Substituting the values of R_{eq} and R_{0eq} from equations (25) and (26) into (27), we obtain:

$$\Delta t_0 \Delta h_0 = \Delta t \Delta h \frac{P^2}{P_0^2} \quad (28)$$

Δt , Δh and P are measured during the experiment for specific humidity value W_v .

Using the relation analogous to the expression (28) the current $\Delta t_i \Delta h_i$ can be obtained from P_i :

$$\Delta t_i \Delta h_i = \Delta t_0 \Delta h_0 \frac{P_0^2}{P_i^2} = \Delta t \Delta h \frac{P^2}{P_i^2} \quad (29)$$

Denoting the air permeability coefficient measured in speed units via K'_i and taking into account the fact that it is associated with K' the air permeability coefficient obtained from equation (15) by the relation:

$$K'_i = K' \rho g \quad (30)$$

from (15), (18), (19) and (29) we obtain the following:

$$K'_{i} = \frac{\Delta V \Delta x}{\Delta t \Delta h S_s P^2} (P_0^2 - P_i^2) \quad (31)$$

The relationship between the air permeability coefficient and hydraulic conductivity coefficient may be obtained from same laws of Darcy and Poiseuille. For the case of pore complete filling with a continuous medium, these laws may be formulated in the following way:

$$Q_1 = K_1 \frac{\Delta P}{\Delta x} S_s, \quad Q_1 = \frac{\pi}{8\eta_1} \frac{\Delta P}{\Delta x} R_{ef}^4 \quad \text{for air} \quad (32)$$

$$Q_2 = K_2 \frac{\Delta P}{\Delta x} S_s, \quad Q_2 = \frac{\pi}{8\eta_2} \frac{\Delta P}{\Delta x} R_{ef}^4 \quad \text{for water} \quad (33)$$

where Q_1 and Q_2 are the consumption rate of air and water, respectively; K_1 and K_2 are the filter coefficients; η_1 and η_2 are the viscosity coefficients. For both media the relations may be formulated:

$$\frac{\pi}{8\eta_1} R_{ef}^4 = K_1 S_s \quad \text{and} \quad \frac{\pi}{8\eta_2} R_{ef}^4 = K_2 S_s \quad (34)$$

from which we obtain the relation between the filter coefficients highlighting and equating constants:

$$\frac{K_1}{K_2} = \frac{\eta_2}{\eta_1} \quad (35)$$

This ratio serves as a scale factor when replacing one continuous medium by another. Then, for the case of water flow through an unsaturated sample, the hydraulic conductivity coefficient is determined by an expression similar to (31):

$$K'_{2i} = \frac{\Delta V \Delta x}{\Delta t \Delta h S_s P^2} \frac{\eta_1}{\eta_2} (P_0^2 - P_i^2) \quad (36)$$

Since $P_i = P_0 - W_{vi}$, where W_{vi} is the current value of volume moisture in unit fractions, then equation (36) may be formulated as:

$$K'_{2i} = \frac{\Delta V \Delta x}{\Delta t \Delta h S_s P^2} \frac{\eta_1}{\eta_2} [P_0^2 - (P_0 - W_{vi})^2] \quad (37)$$

where ΔV , Δx , Δt , Δh , S_s , P are measured values; η_1 and η_2 are constants; W_{vi} is a defined value.

Equation (37) expresses the relation between the coefficient of hydraulic conductivity and volumetric moisture. The boundary conditions of equation (33) are: $P_i = 0$ is the case of complete filling of a continuous medium; $P_i = P_0$ when the pores are completely free. For the first case, the coefficient of the hydraulic conductivity coefficient is equal to the infiltration coefficient:

$$K'_2 = \frac{\Delta V \Delta x}{\Delta t \Delta h S_s P^2} \frac{\eta_1}{\eta_2} P_0^2 \quad (38)$$

For the second (dry sample), $K'_2 = 0$.

APPLICATION AND RESULTS

Based on the above facts, we have examined, under field conditions, the basic zonal soils of the Eastern European Plains with various erosion degrees and used the proposed methodology to determine their degree of erosion: soddy-podzolic soils, gray forest soils, leached black earth, based on the infiltration coefficient, porosity and bulk density changes (Tables 1, 2, 3). It is possible that in other areas such data may differ from those listed below (due to the change of soil-

Table 1 Diagnostic table to determine the erosion of soddy-podzolic soils.

Soil erosion degree	Filtration coefficient change (%)	Porosity change (%)		Volume weight change (%)
Absent	–	–	–	–
Weak	0 – (–40)	0 – (–15)	0 – (–2)	0 – (+10)
Average	–40 – (–80)	–15 – (–25)	–2 – (–25)	+10 – (+20)
Strong	–80 – (–95)	–25 – (–50)	–25 – (–50)	+20 – (+30)
Distance from the surface	0–20	0–20	20–40	0–20

Table 2 Diagnostic table to determine the erosion of gray forest soils.

Soil erosion degree	Filtration coefficient change (%)			Porosity change (%)			Volume weight change (%)	
Absent	–	–	–	–	–	–	–	–
Weak	0–(-10)	0–(-25)	0–(-40)	0–(-2)	0–(-1)	0–(-1)	0–(+2)	0–(+2)
Average	-10–(-25)	-25–(-35)	-40–(-50)	-2–(-4)	-1–(-5)	-1–(-3)	+2–(+7)	+2–(+4)
Strong	>(-25)	>(-35)	>(-50)	>(-4)	>(-5)	>(-3)	>(+7)	>(+4)
Distance from the surface	0–20	20–40	40–60	0–20	20–40	40–60	0–20	20–40

Table 3 Diagnostic table to determine the erosion of leached chernozem.

Soil erosion degree	Filtration coefficient change (%)		Porosity change (%)		Volume weight change (%)	
Absent	–	–	–	–	–	–
Weak	0 – (-50)	0 – (-50)	0 – (-18)	0 – (-18)	0 – (+13)	0 – (+8)
Average	-50 – (-95)	-50 – (-95)	-18 – (-22)	-18 – (-22)	+13 – (+26)	+8 – (+25)
Strong	>(-95)	>(-95)	>(-22)	>(-22)	>(+26)	>(+25)
Distance from the surface	0–20	20–40	0–20	20–40	0–20	20–40

making rocks). The main indicator in the diagnostic tables is the infiltration coefficient; porosity and bulk density are optional. The benchmarks are the humus content in soil determined by the Zaslavsky method (1979), as well as morphological parameters determined according to the method developed by Sobolev (1954).

CONCLUSIONS

This study has shown the principles of the possibility of application of the infiltration coefficient and porosity, as a specific field method for the study of aerodynamic similarity degree of erosion of soil. The advantage over traditional methods is the more precise gradation levels of erosion, based on a precise quantitative indicators rather than visual morphological characteristics. With certain adaptation and validation in the field, this method is applicable to diagnose the degree of erosion of zonal soils of other territories.

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